

# lecture X - MOTORS 101

How does a motor spin? And how do we *design circuits* that can make them spin using PCBs?

# Outline for Today

- **Modeling motors (4-magnet model)**
- **Brushed vs brushless motors**
- **Circuit model of a motor, brushed + brushless models**
- **3-coil version of BLDC motors**
- **Field-Oriented Control (visually), Clarke+Park transforms**

**(Our goal is to teach you Field-Oriented Control today which is a technique for controlling three-phase, brushless motors)**

# Designing a Motor Controller.

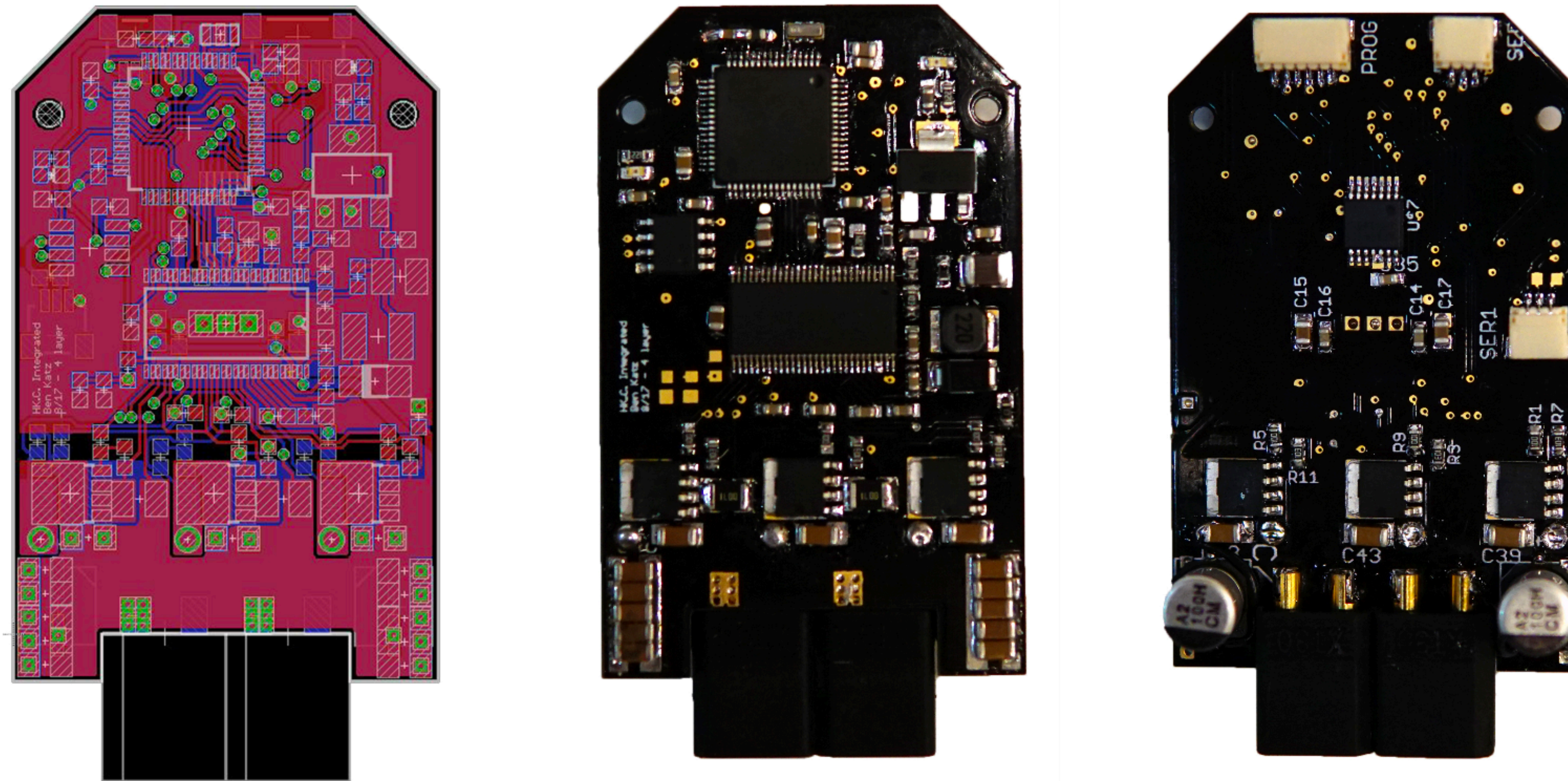
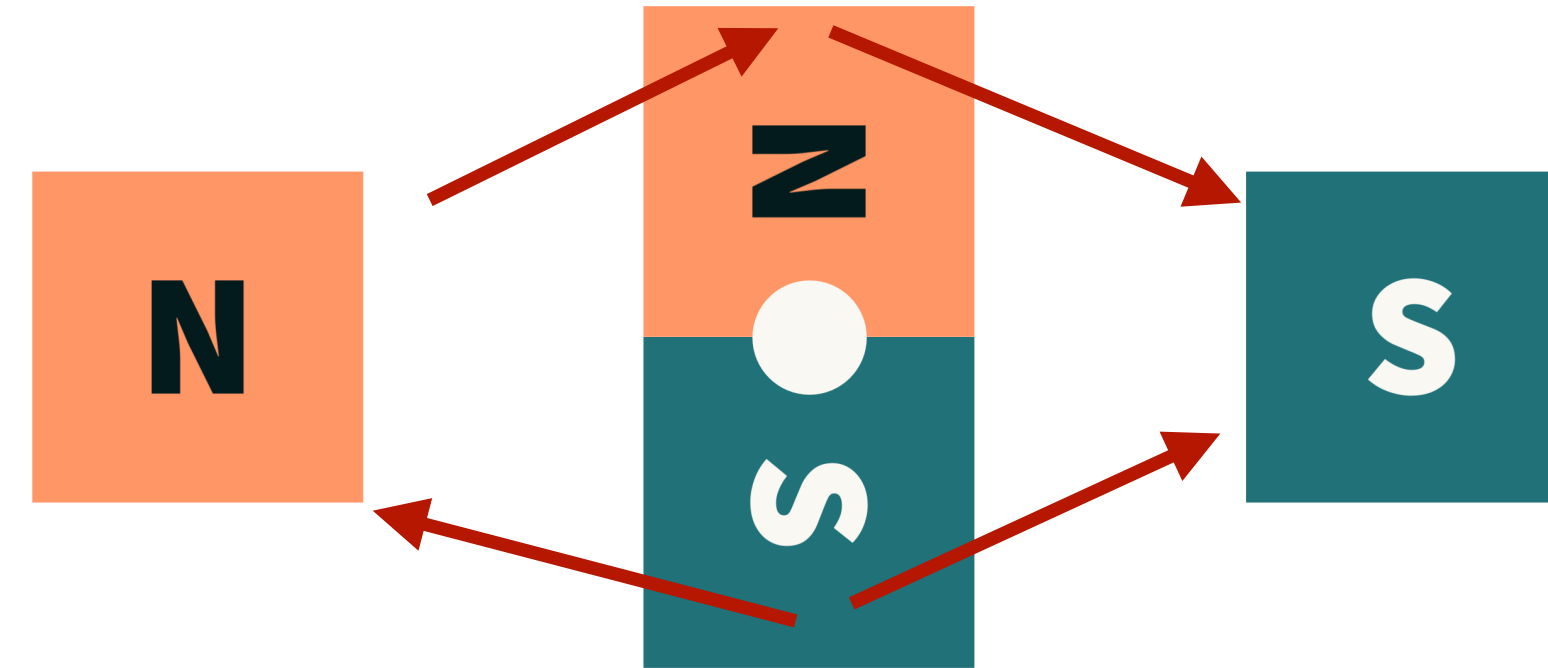


Figure 2-10: PCB layout, front, and back of the inverter.

**DEMOS!!!**

# 4-magnet model of a motor

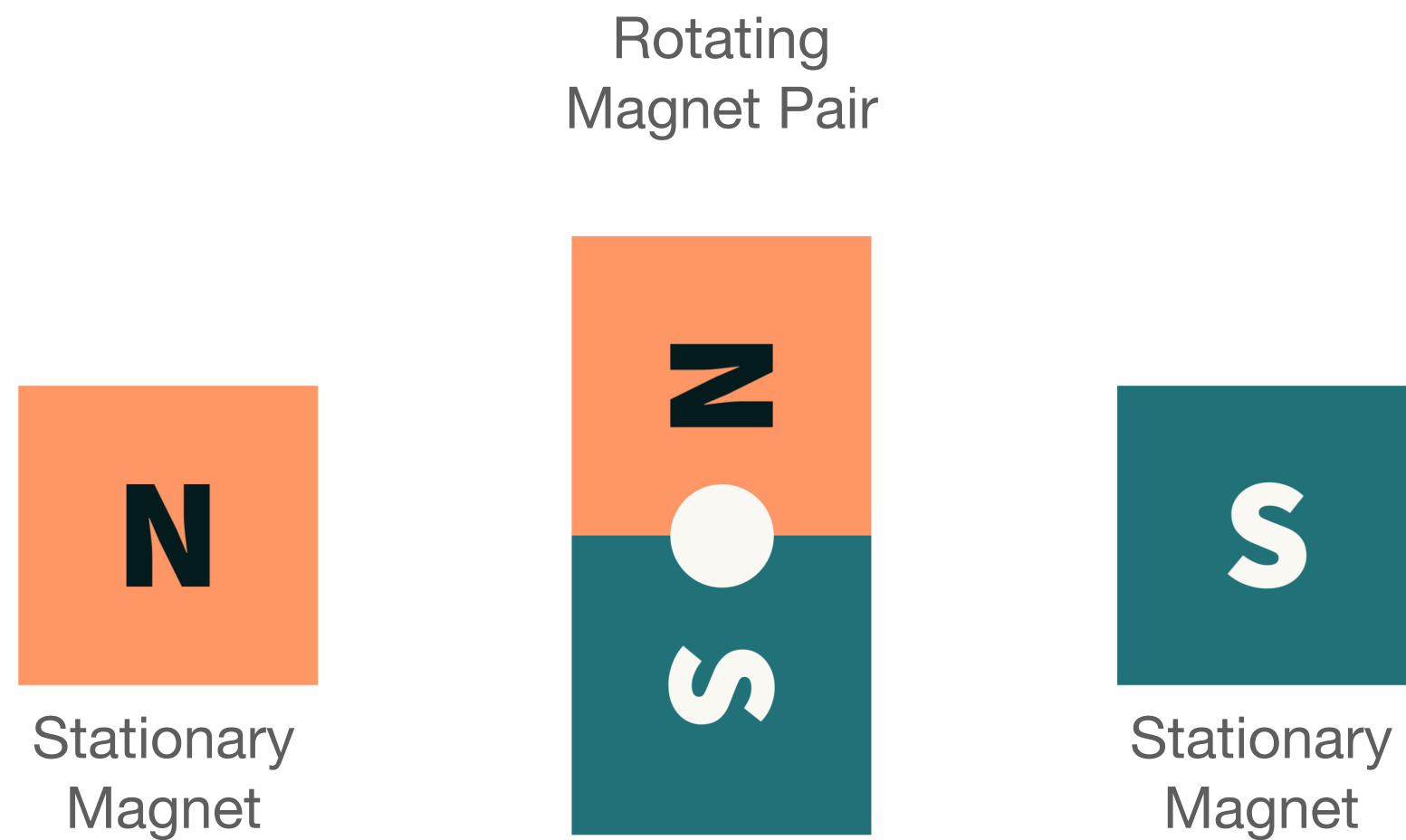
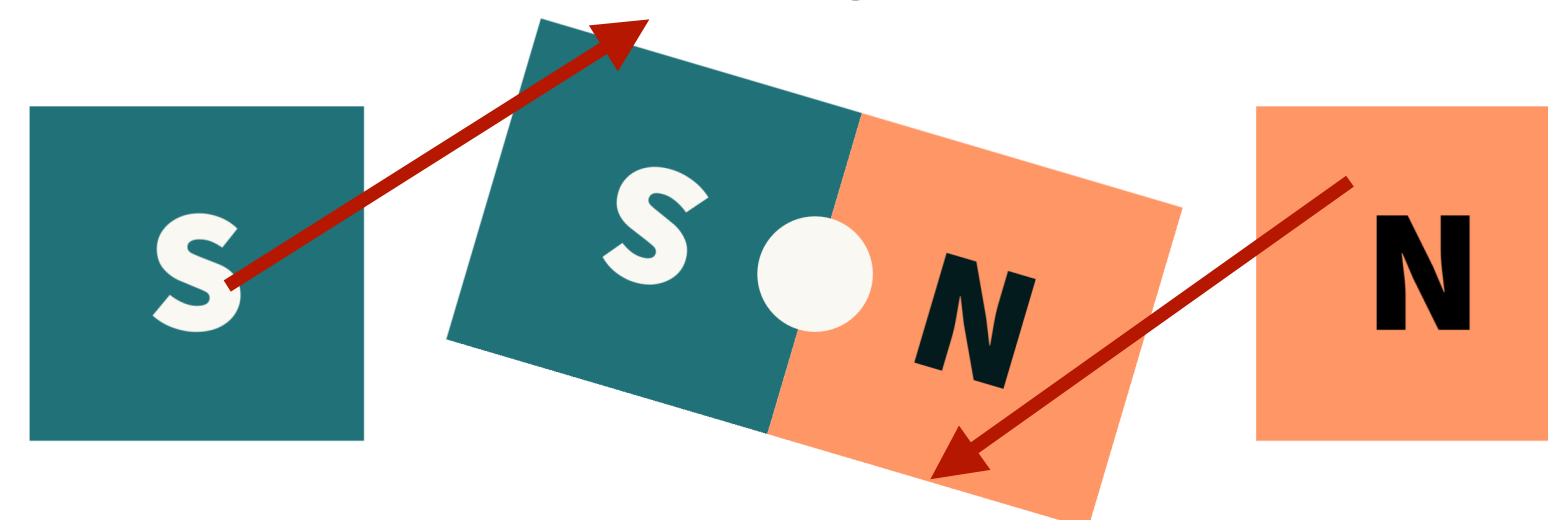
Forces between magnets produces a torque



As the magnet rotates the force becomes more horizontal, when the force is horizontal the magnet would stop moving if we left it like this. Imagine the forces as strings pulling the magnet, the magnet would stop.



But if we SWITCH the magnets, S now repels S, N repels N, and the motor can keep spinning!

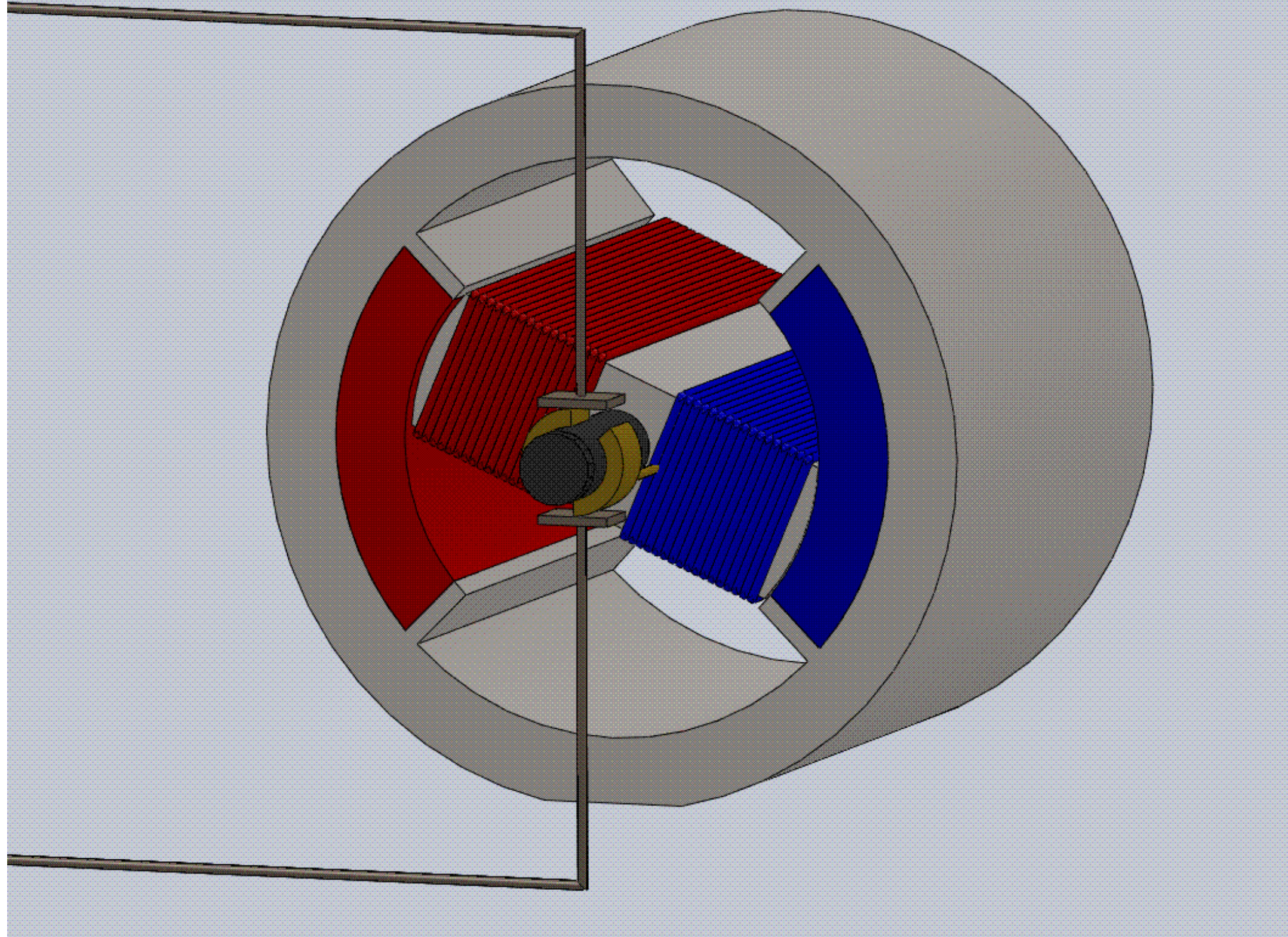


# The 4 Horsemen of



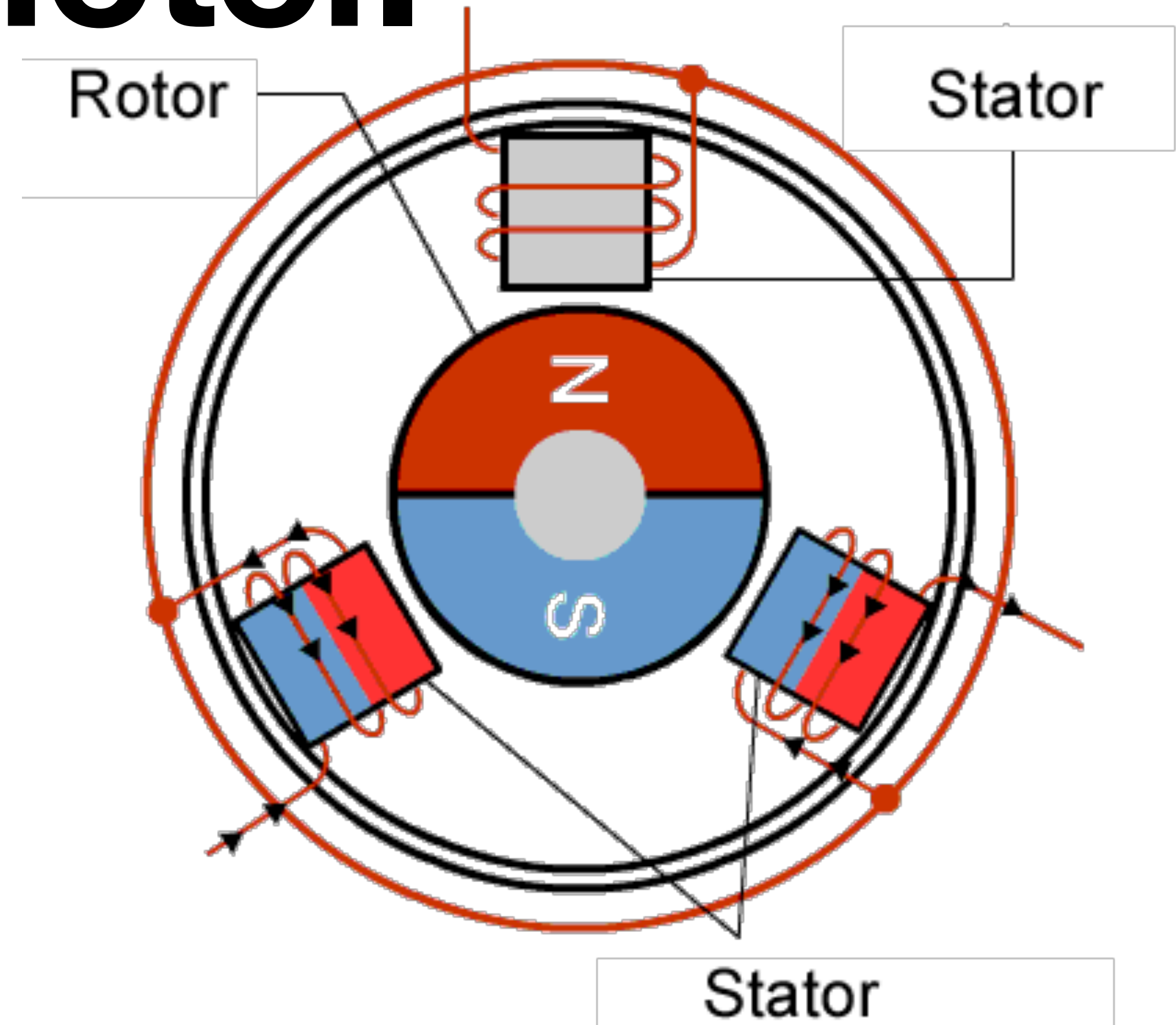
# Ok but like, how do we do?

# Brushed Motor.



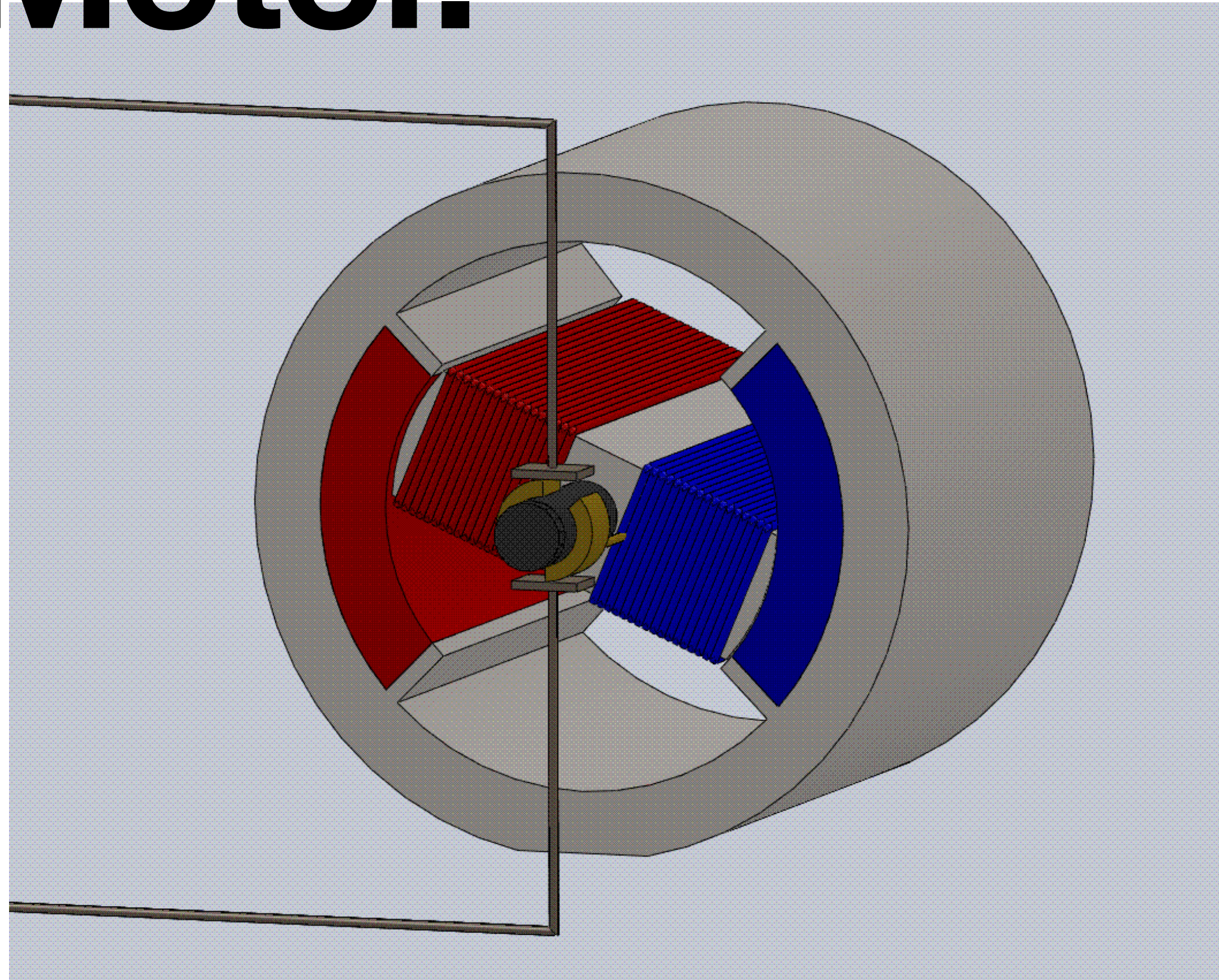
<https://cecas.clemson.edu/cvel/auto/actuators/motors-dc-brushed.html>

# Brushless Motor.



<https://www.renesas.com/us/en/support/engineer-school/brushless-dc-motor-01-overview>

# Brushed Motor.



<https://cecas.clemson.edu/cvel/auto/actuators/motors-dc-brushed.html>

# Brushless



NEED A MOTOR CONTROLLER TO OPERATE AND SWITCH THE FIELD (THIS IS WHAT YOU ARE DESIGNING IF YOU ARE DOING THE VESC PROJECT).

Stator

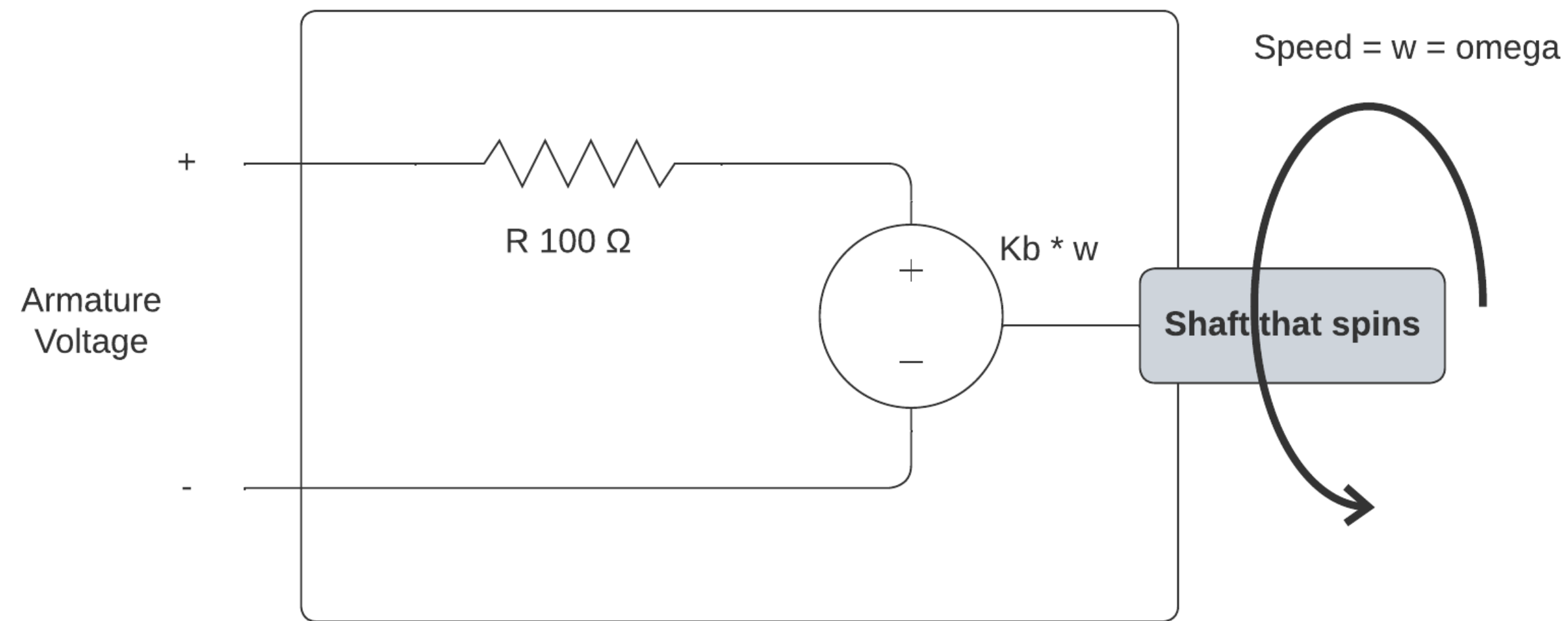
<https://www.hobbytown.com/spektrum-rc-firma-130-amp-sensorless-brushless-smart-esc-motor-combo-1900kv-spmxsemc04/p1222229>



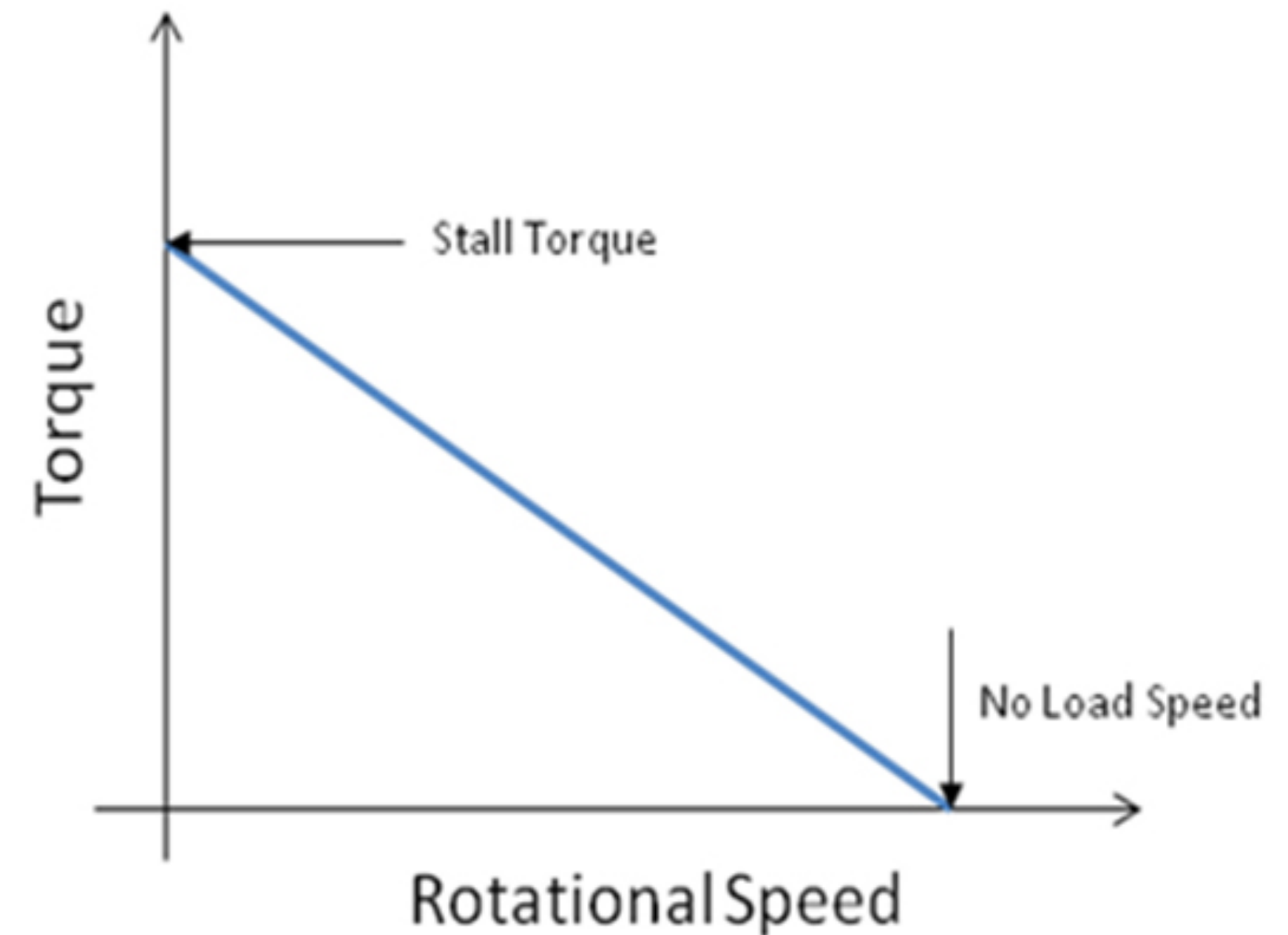
# Circuit Model of a Motor.

$$V = k_b * \omega$$

$$T = k_t * I$$



**(Note how the max speed depends on the armature voltage)**



# Practical Aside.

**(Brushed motors also have motor controllers that allow you to control the speed of the motor)**

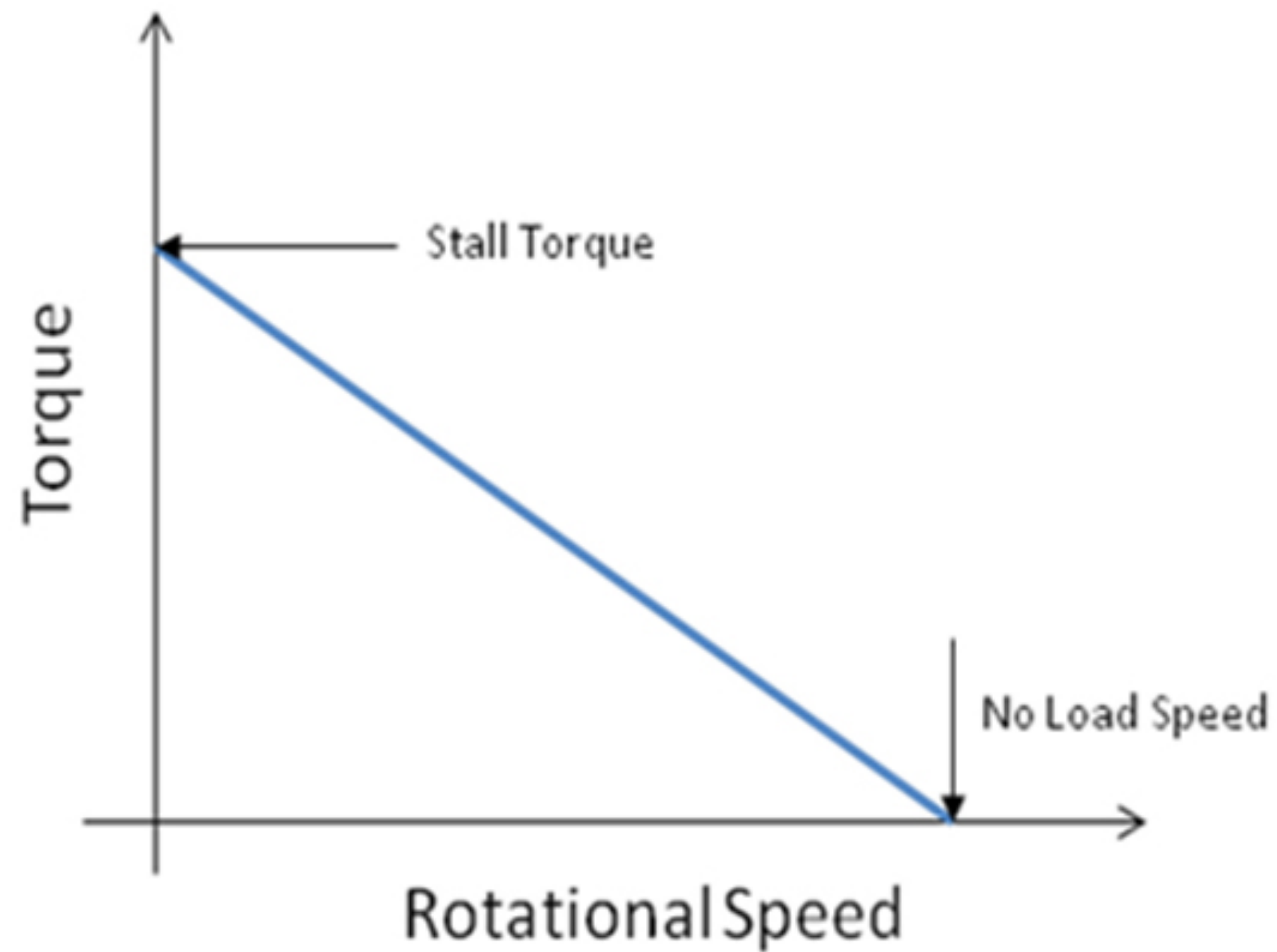
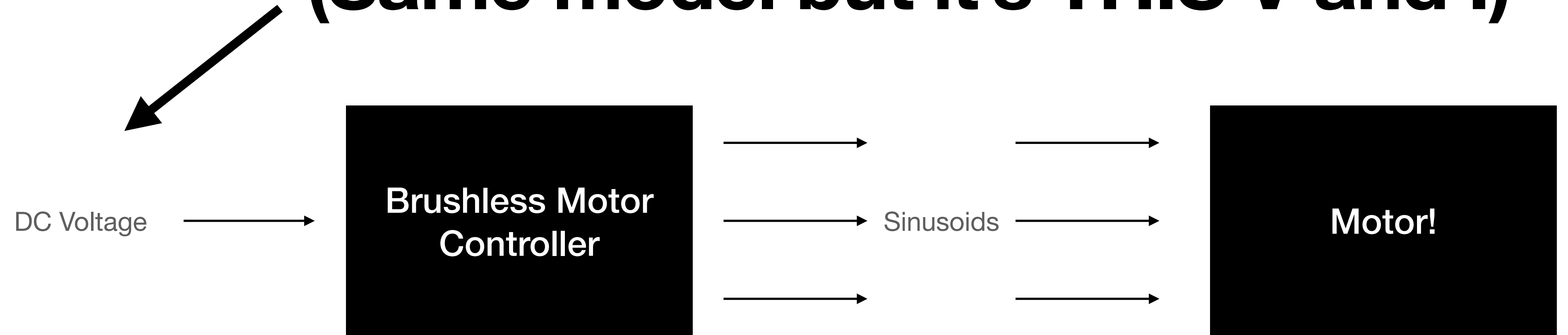
**(These work by taking in a DC voltage from a source, and then varying the armature voltage)**

**(Then, the torque-speed max speed point is dependent on the DC input voltage)**



# Modeling Brushless Motors.

(Same model but it's THIS V and I)



$$V = k_b * \omega$$

$$T = k_t * I$$

# Field-Oriented-Control, of brushless motors!

# This is a Brushless Motor.



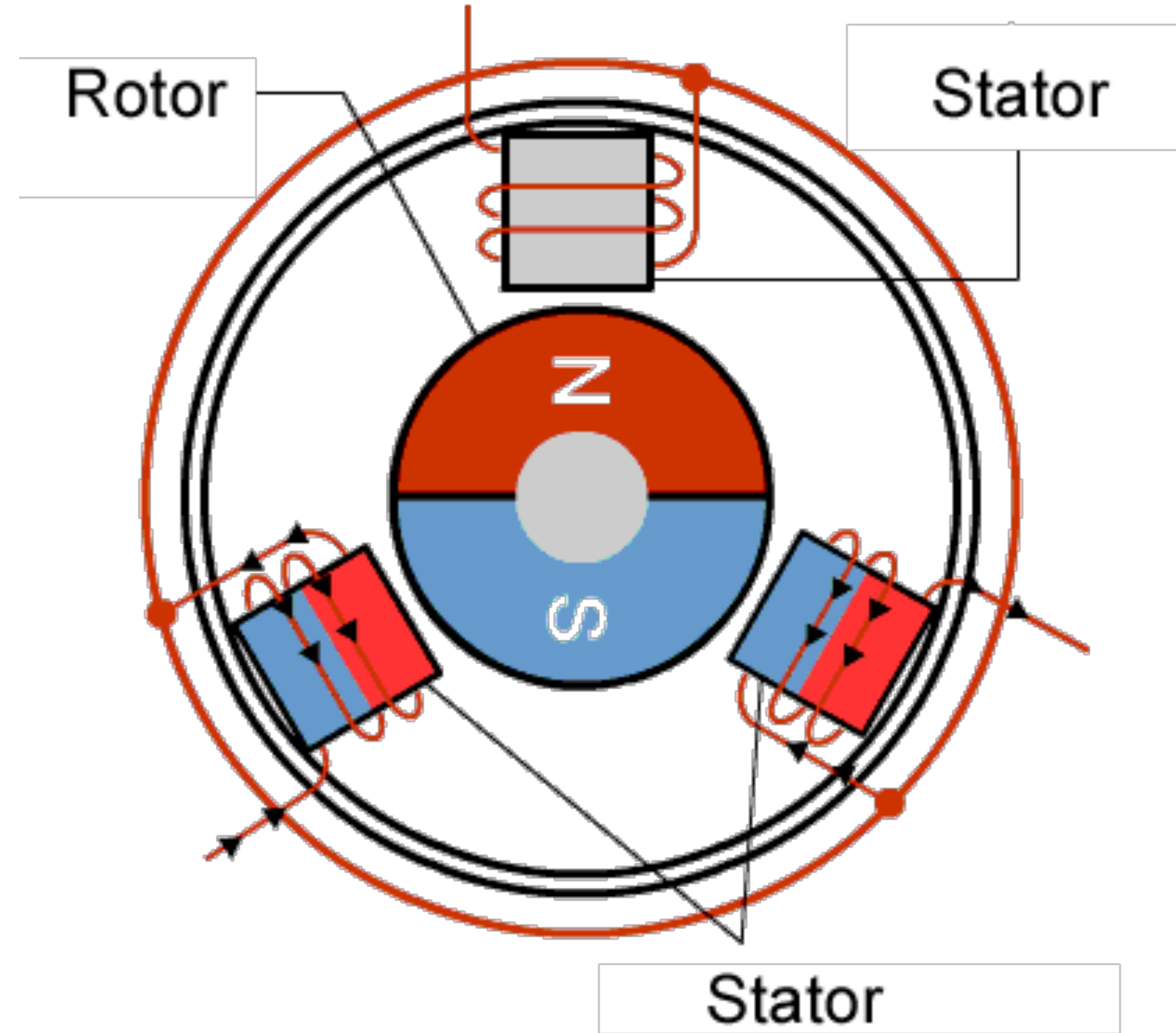
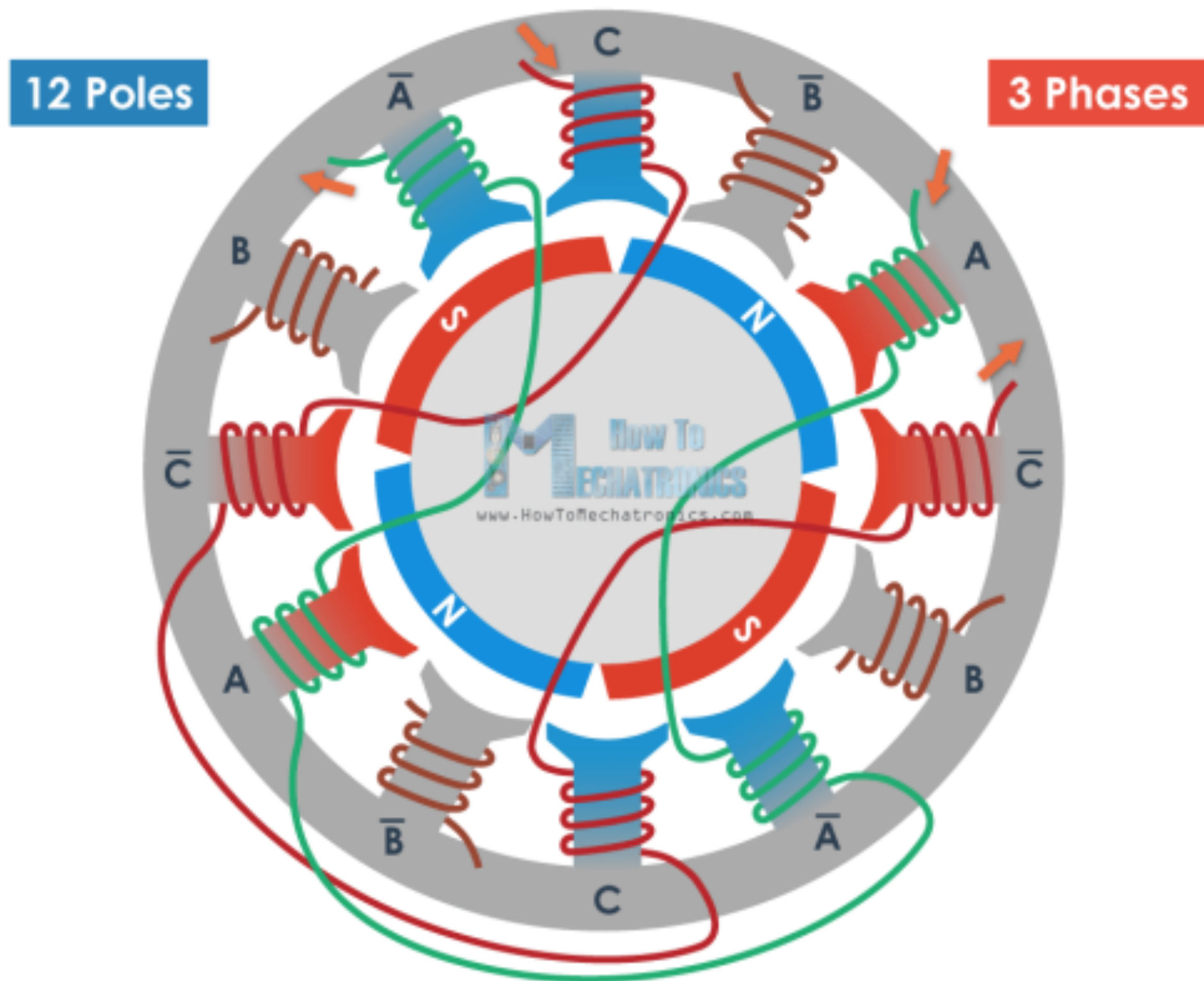
**(pole pairs is the number of pairs of magnets on the rotor)**

**(Slots is the number of coils in the stator)**

# This is a Brushless Motor.

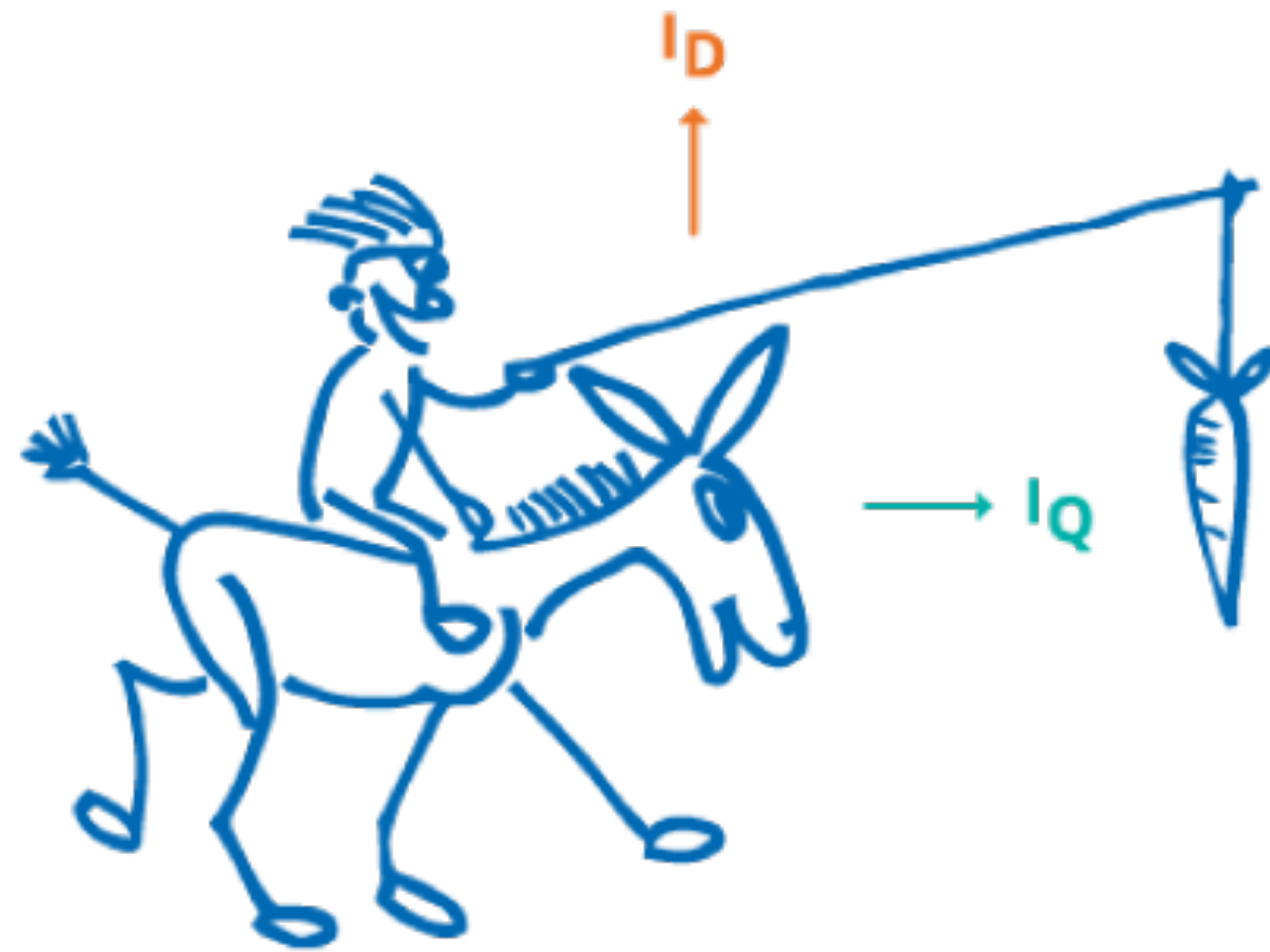
(Phases have a pattern, and they alternate, this depends on motor design)

Brushless DC Motor Working Principle

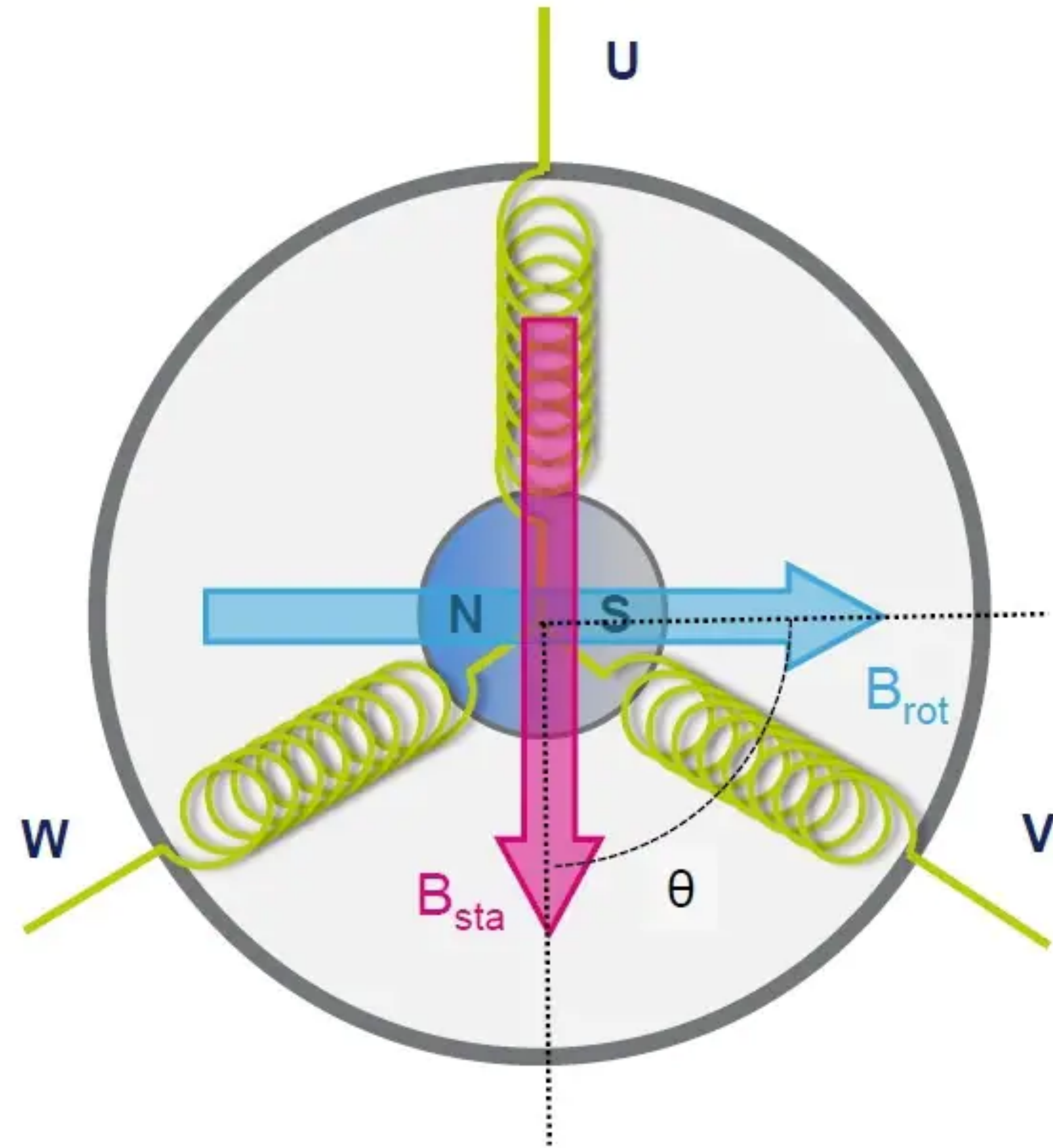


(But ALL motors can be simplified into this model)

# Field-Oriented Control.

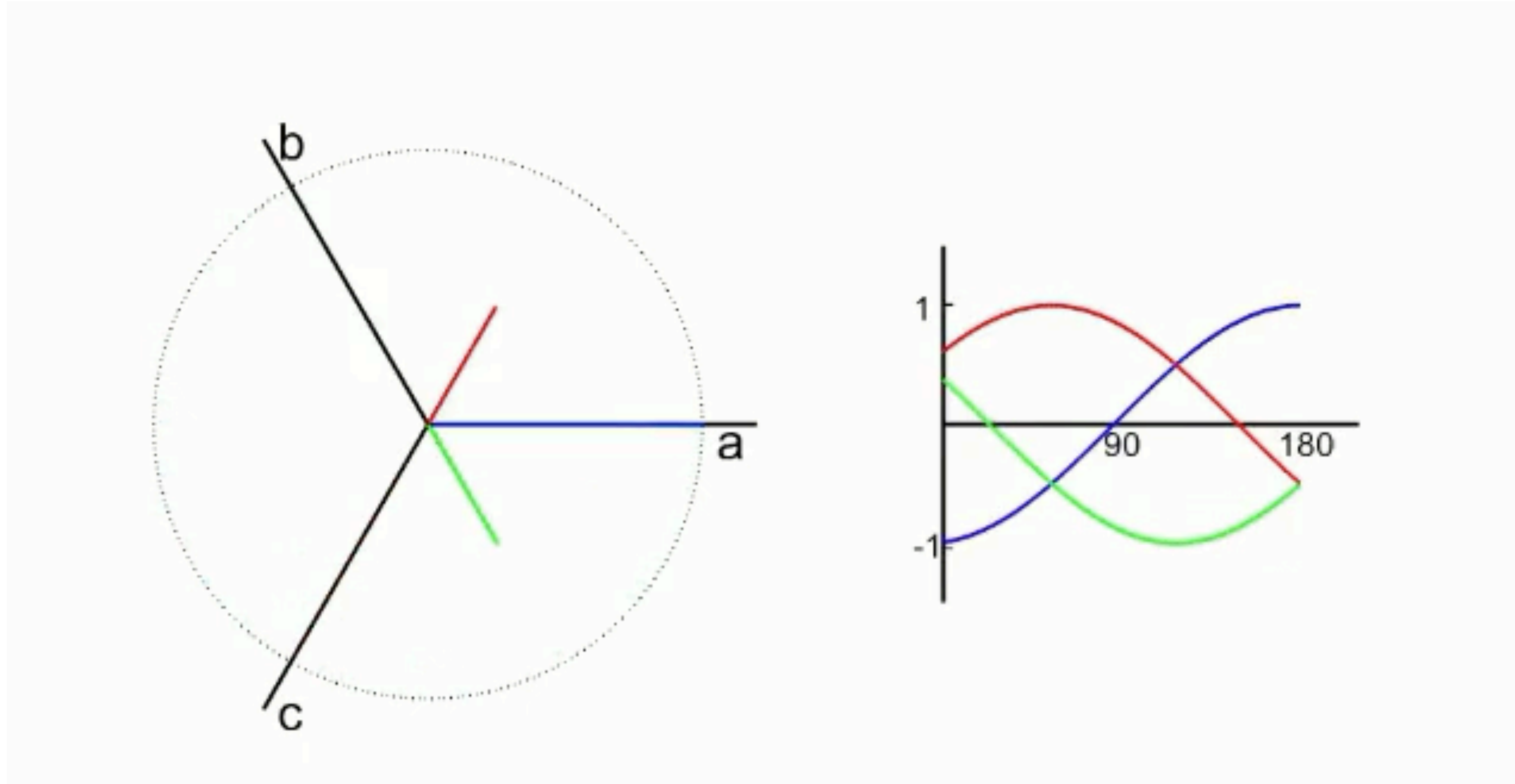


<https://www.trinamic.com/technology/motor-control-technology/field-oriented-control/>



<https://www.st.com/en/applications/industrial-motor-control/3-phase-field-oriented-control-foc.html>

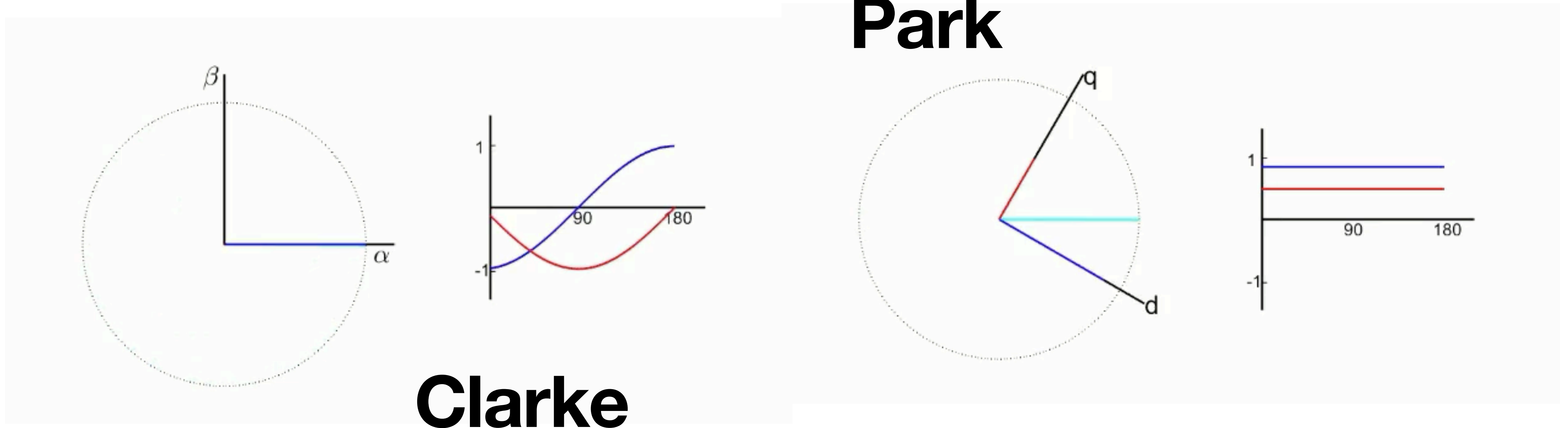
# Field-Oriented Control.





# Clarke + Park Transform.

-Mathworks



Clarke

Park

(Edith Clarke was the first woman to deliver a paper at the [American Institute of Electrical Engineers](#), the first female engineer whose professional standing was recognized by [Tau Beta Pi](#), and the first woman named as a Fellow of the [American Institute of Electrical Engineers.](#)) - AND SHES FROM MIT!

-Wikipedia

# Clarke + Park Transform.

-Texas Instruments

## 3.1 Mathematical Clarke transform.

The mathematical transformation called Clarke transform modifies a three-phase system to a two-phase orthogonal system:

$$i_{\alpha} = \frac{2}{3} \cdot i_a - \frac{1}{3}(i_b - i_c)$$

$$i_{\beta} = \frac{2}{\sqrt{3}}(i_b - i_c)$$

$$i_o = \frac{2}{3}(i_a + i_b + i_c)$$

**STAR NODE**  
**→ Kirchoff's**  
**Current Law**

with  $i_{\alpha}$  and  $i_{\beta}$  components in an orthogonal reference frame and  $i_o$  the homopolar component of the system.

## 3.2 Mathematical Park transform.

The two phases  $\alpha$ ,  $\beta$  frame representation calculated with the Clarke transform is then fed to a vector rotation block where it is rotated over an angle  $\theta$  to follow the frame d,q attached to the rotor flux.

The rotation over an angle  $\theta$  is done according to the formulas:

$$i_{sd} = i_{\alpha} \cdot \cos(\theta) + i_{\beta} \cdot \sin(\theta)$$

$$i_{sq} = -i_{\alpha} \cdot \sin(\theta) + i_{\beta} \cdot \cos(\theta)$$

# Clarke

# Park

# Clarke + Park Transform.

-Texas Instruments

### 3.3 Mathematical Inverse Park and Clarke transforms.

The vector in the d, q frame is transformed from d, q frame to the two phases  $\alpha$ ,  $\beta$  frame representation calculated with a rotation over an angle  $\theta$  according to the formulas:

$$i_{\alpha} = i_{sd} \cdot \cos(\theta) - i_{sq} \cdot \sin(\theta)$$

$$i_{\beta} = i_{sd} \cdot \sin(\theta) + i_{sq} \cdot \cos(\theta)$$

The modification from a two-phase orthogonal  $\alpha$ ,  $\beta$  frame to a three-phase system is done by the following equations:

$$i_a = i_{\alpha}$$

$$i_b = -\frac{1}{2} \cdot i_{\alpha} + \frac{\sqrt{3}}{2} \cdot i_{\beta}$$

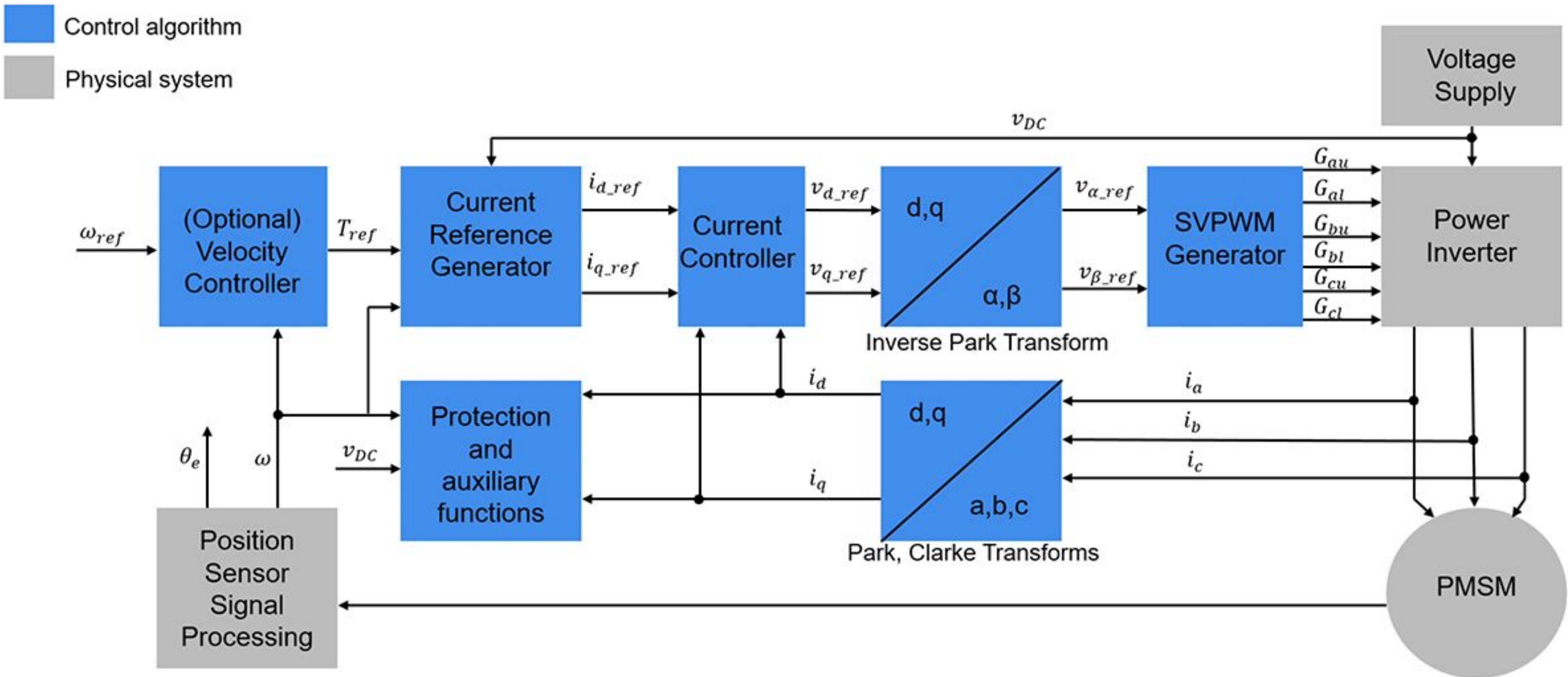
$$i_c = -\frac{1}{2} \cdot i_{\alpha} - \frac{\sqrt{3}}{2} \cdot i_{\beta}$$

### 3.4 Transforms summary.

<b>Park</b>	<b>Inverse Park</b>
<b>a, b, c -&gt; <math>\alpha, \beta</math></b>	<b>d, q -&gt; <math>\alpha, \beta</math></b>
$i_{\alpha} = \frac{2}{3} \cdot i_a - \frac{1}{3} (i_b - i_c)$ $i_{\beta} = \frac{2}{\sqrt{3}} (i_b - i_c)$ $i_o = \frac{2}{3} (i_a + i_b + i_c)$ $\Rightarrow$ $i_{\alpha} = i_a$ $i_{\beta} = \frac{1}{\sqrt{3}} \cdot i_a + \frac{2}{\sqrt{3}} i_b$ $i_a + i_b + i_c = 0$	$i_{\alpha} = i_{sd} \cdot \cos(\theta) - i_{sq} \cdot \sin(\theta)$ $i_{\beta} = i_{sd} \cdot \sin(\theta) + i_{sq} \cdot \cos(\theta)$
<b><math>\alpha, \beta</math> -&gt; d, q</b>	<b><math>\alpha, \beta</math> -&gt; a, b, c</b>
$i_{sd} = i_{\alpha} \cdot \cos(\theta) + i_{\beta} \cdot \sin(\theta)$ $i_{sq} = -i_{\alpha} \cdot \sin(\theta) + i_{\beta} \cdot \cos(\theta)$	$i_a = i_{\alpha}$ $i_b = -\frac{1}{2} \cdot i_{\alpha} + \frac{\sqrt{3}}{2} \cdot i_{\beta}$ $i_c = -\frac{1}{2} \cdot i_{\alpha} - \frac{\sqrt{3}}{2} \cdot i_{\beta}$

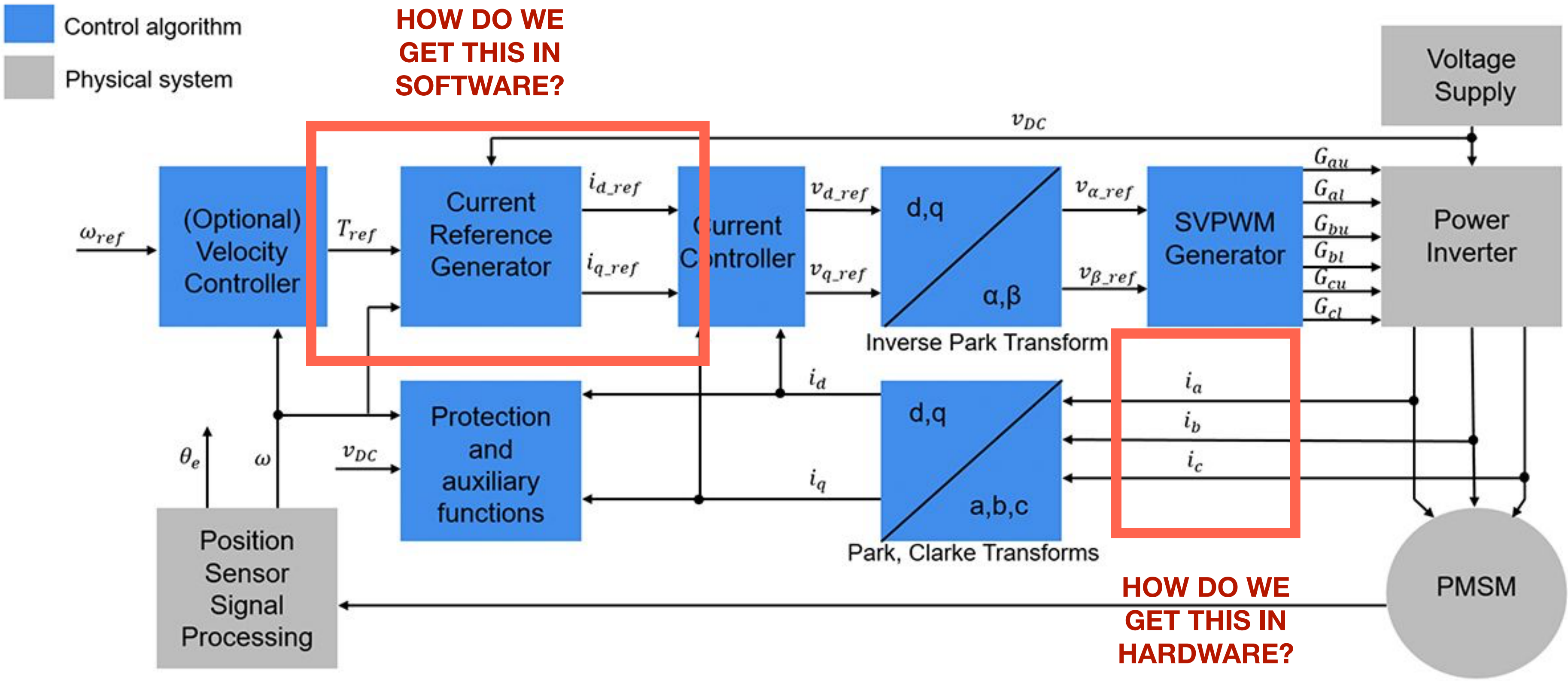
# FOC as a block-set.

-Mathworks



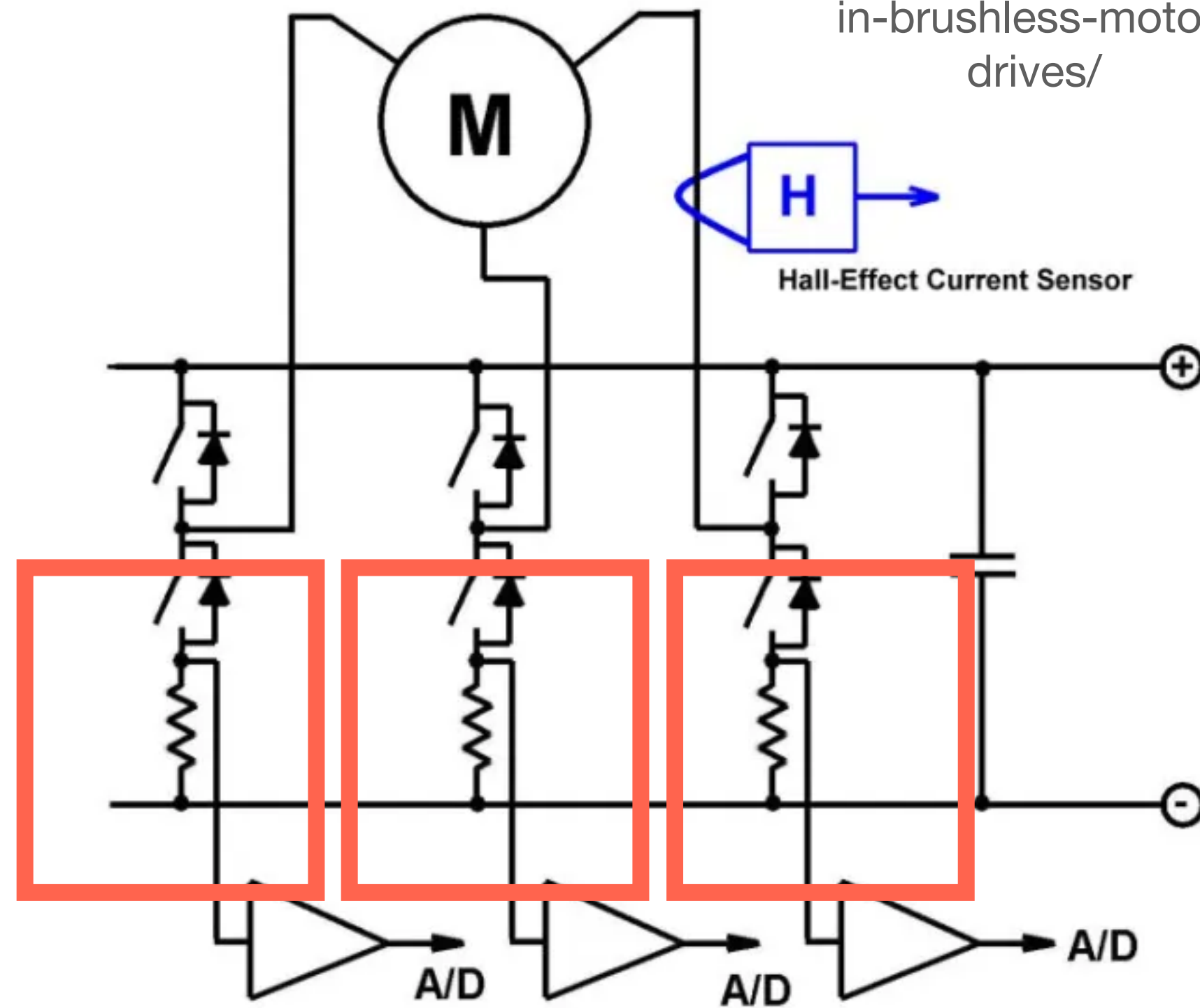
# FOC as a block-set.

-Mathworks



# Phase Current Measurement + The DRV Chip.

<https://www.powerelectronicsnews.com/current-sensing-in-brushless-motor-drives/>



(A good alternative is the trinamic series)

## 8.2 Functional Block Diagram

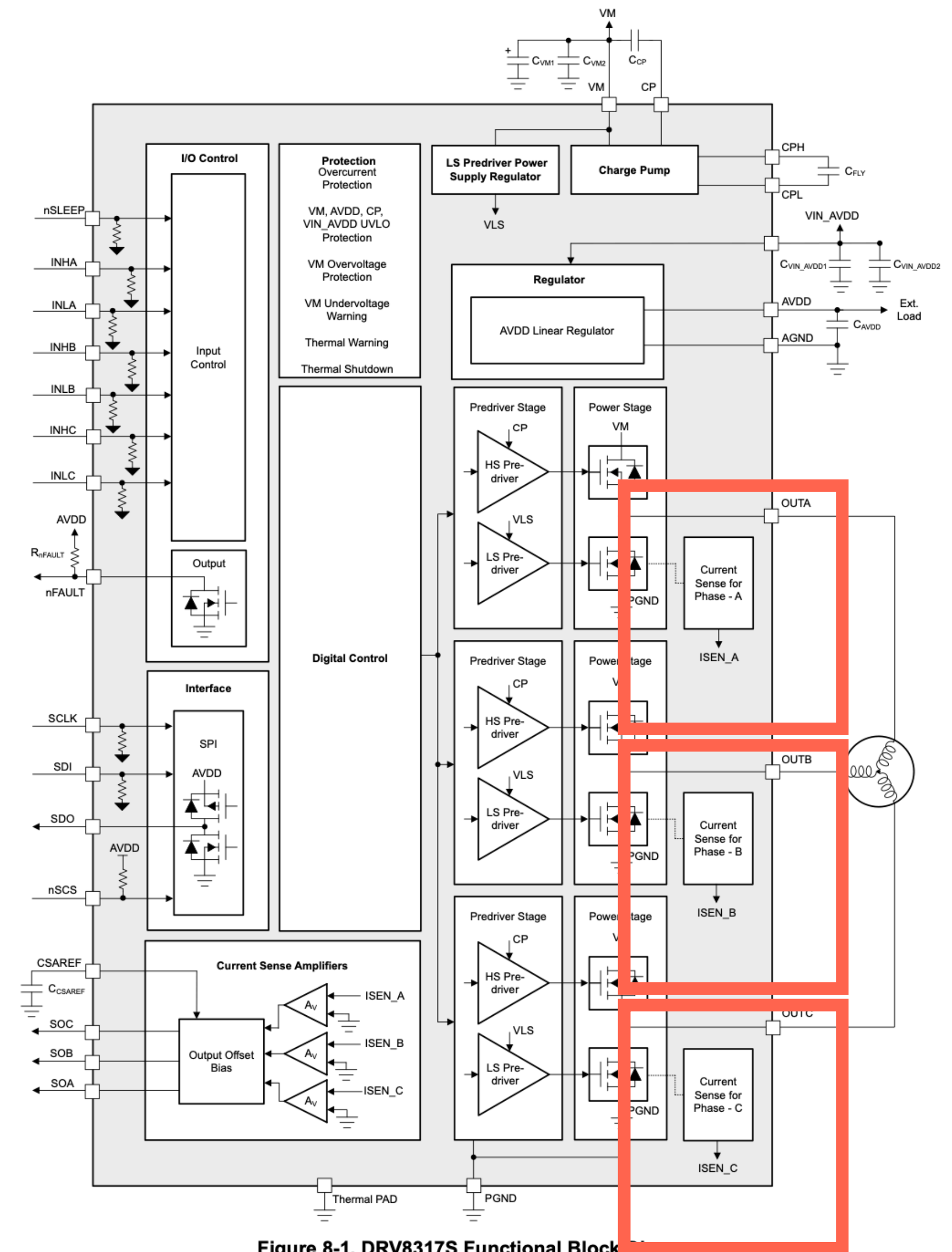


Figure 8-1. DRV8317S Functional Block Diagram

# How to get $i_d$ ? And $i_q$ ?

(Remember  $i_q$  is the torque-producing current)

<https://www.mathworks.com/help/sps/ref/pmsmcurrentreferencegenerator.html>

<https://www.mathworks.com/help/sps/ref/pmsm.html>

For the ZDAC method, the block sets the  $d$ -axis current reference  $i_d^{ref}$  to zero and determines the  $q$ -axis current reference  $i_q^{ref}$  using the torque equation:

$$i_d^{ref} = 0,$$

and

$$i_q^{ref} = \frac{2T_{ref}}{3p\psi_m},$$

where:

- $T_{ref}$  is the reference torque input.
- $p$  is the number of pole pairs.
- $\psi_m$  is the permanent magnet flux linkage.

(Comes from data sheet, motor testing, calculating, it can also be estimated).

$$k_e = N\psi_m. \quad k_t = N\psi_m.$$

(We can get  $K_t$  and  $K_b$  from motor testing!)

(Comes from motor testing and desired torque).

# **VESC Schematic. PDF**

**([https://vesc-project.com/sites/default/files/Benjamin%20Posts/VESC\\_6.pdf](https://vesc-project.com/sites/default/files/Benjamin%20Posts/VESC_6.pdf))**



# FOC as a block-set.

-Mathworks

